Math 1131 Week 8 Worksheet

Name: ________________________

Discussion Section:_____________

Solutions should show all of your work, not just a single final answer.

4.1: Maximum and Minimum Values

1. For the following functions, find all critical numbers **exactly**.

   (a) $f(x) = x^5 - 2x^3$

   (b) $f(x) = x - 2\sin x$ for $-2\pi < x < 2\pi$

   (c) $f(x) = e^{-x} - e^{-3x}$ for $x > 0$

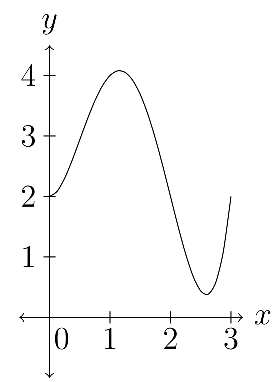
2. Use calculus to find the absolute maximum and minimum values of the following functions on the given intervals. Give your answers **exactly** and show supporting work.

   (a) $f(x) = x^3 - 2x^2 + x + 1$ on $[0, 1]$

   (b) $f(x) = x^4 - 2x^2 + 4$ on $[0, 2]$

   (c) $f(x) = (7x - 1)e^{-2x}$ on $[0, 1]$

3. Below is the graph of $f(x) = x^4 - 5x^3 + 6x^2 + 2$. On the interval $[0, 3]$ determine the maximum and minimum value of the *slope* of the graph, *i.e.*, the maximum and minimum values of $g(x) = f'(x)$.



4. T/F (with justification) If $f(x)$ is a differentiable function on (a, b) and $f(x)$ has a local maximum or minimum value at $x = c$ in (a, b) then $f'(c) = 0$.

5. T/F (with justification) If $f(x)$ is a differentiable function on (a, b) and $f'(c) = 0$ for a number c in (a, b) then $f(x)$ has a local maximum or minimum value at $x = c$.

4.2: Mean Value Theorem

6. Find every number c that satisfies the conclusion of the Mean Value Theorem for the function $f(x) = x^3 - 4x^2 - 5$ on the interval $[1, 2]$.

7. T/F (with justification) The function $1 - \dfrac{1}{x^4}$ satisfies the hypotheses of Rolle's Theorem on the interval $[-1, 1]$.

8. T/F (with justification) The graph of the semicircle on $[-1, 1]$ below fits the hypotheses of the Mean Value Theorem.